## THE OPEN UNIVERSITY OF SRI LANKA B.Sc./B.Ed DEGREE PROGRAMME - LEVEL 05 NO BOOK TEST-2023/2024 APPLIED MATHEMATICS ADU5307 — Numerical Methods



**DURATION: ONE HOUR** 

Date: 03. 09. 2023

Time: 2.30 p.m. -3.30 p.m.

## ANSWER ALL QUESTIONS.

- 1. Evaluate  $\int_0^1 x^3 dx$  correct up to four decimal places using Trapezoidal rule by considering five sub-intervals. Also, find the value of the integral by using analytical method. Hence find the absolute error.
- 2. Applying Taylor series method of fourth-order for the differential equation y'' + xy = 0 subjected to initial conditions y(0) = 1 and y'(0) = 0.5, evaluate the y(0.1) correct to four decimal places.
- 3. Using Picard's method of  $3^{rd}$  approximation solve  $y' + y = e^x$ , with the initial condition y(0) = 0. Hence find the value of y(0.1).
- 4. Given the initial value problem that  $\frac{dy}{dx} = 3x^2 + 1$ , with the initial condition y(1) = 2. Estimate y(2), by using Euler's method when h = 0.25.