THE OPEN UNIVERSITY OF SRI LANKA

B.Sc. /B.Ed DEGREE PROGRAMME - LEVEL 04

CONTINUOUS ASSESSMENT TEST 1(CAT 1) -2021/2022

ADU4303/ADE4303 - Applied Linear Algebra and Differential Equations



DURATION: ONE HOUR

Date: 07.01.2023

Time: 09.00 a.m. - 10.00 a.m.

ANSWER ALL QUESTIONS.

1. Determine the rank of the following matrix:

$$\begin{pmatrix}
-2 & -1 & -3 & -1 \\
1 & 2 & 3 & -1 \\
1 & 0 & 1 & 1 \\
0 & 1 & 1 & -1
\end{pmatrix}$$

2. (i) Find the adjoint of the co-efficient matrix (A) of the following system of equations:

$$x+2y+3z=2$$
$$2x+4y+5z=3$$
$$3x+5y+6z=3$$

- (ii) Hence find the inverse of matrix A and also, find the solution of the system of equations in part (i).
- 3. Verify the Cayley Hamilton Theorem for the matrix B, where

$$B = \begin{pmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{pmatrix}.$$

Hence find B^4 .

4. Find the eigen values and eigen vectors of the following matrix.

$$\begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}.$$